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# First-principle investigations of nitrogen-, boron-, phosphorus-doped graphite electrodes for vanadium redox flow batteries

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# ABSTRACT

An issue that limits the large-scale application of vanadium redox flow batteries (VRFBs) is their low power density, which is associated with the slow reaction kinetics of vanadium redox couples. To enhance the activities of the electrode toward vanadium redox couples, modifying carbon electrode surfaces with heteroatom doping is an effective strategy. In this work, we investigate the catalytic activity of nitrogen (N), boron (B) and phosphorus (P) doped graphite electrodes for VRFBs via density functional theory calculations. A layer of graphene is adopted to represent the surface of a graphite electrode. It is found that water adsorption is stronger with hydrogenated pyridinic N-doped and pyrrolic N-doped graphene than that of graphitic N-, B- and P-doped graphene, while the density of state of all the modified graphene remains metallic features. These results indicate good wettability and electronic conductivity of heteroatom doped graphite electrodes for VRFBs. To further evaluate their catalytic activity towards the  $V^{2+}/V^{3+}$  redox reaction, the metrics of energy difference between inner-sphere and outer-sphere adsorption modes for  $V(H_2O)_6^{3+}$  and  $V(H_2O)_6^{3+}$  and  $V^{3+}$  ions can be significantly improved, suggesting a promising method for developing carbon electrodes for VRFBs.

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# 1. Introduction

Vanadium redox flow batteries (VRFBs) are energy storage devices which provide a promising solution to tackle challenges associated with the intermittent nature of solar energy and wind energy [1-3]. In VRFBs, electrolytes containing dissolved vanadium redox species flow through an electrochemical cell of porous carbon electrodes to lose or gain electrons [4–7]. The electrochemical reaction in VRFBs can be expressed as  $discharge VO^{2+} + H_2O$  at the positive elec- $VO_2^+ + 2H^+ + e^- \equiv$ charge  $\Rightarrow$  discharge  $V^{3+} + e^{-}$  at the negative electrode. trode, and  $V^{2+}$  ==== charge The striking features of VRFBs include long lifetime, high energy efficiency, low maintenance cost, separately designed power and energy capacity, reduced crossover contamination, etc. However, one of the major barriers that limits the large-scale commercialization of VRFBs is their low power density, which is associated with the slow reaction kinetics of vanadium redox couples. An approach to overcoming power density limitation of VRFBs is to modify the

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https://doi.org/10.1016/j.electacta.2019.01.109 0013-4686/© 2019 Elsevier Ltd. All rights reserved. carbon electrode surface so that its electrochemical activities can be enhanced [8-11]. These surface treatments include structural modification, thermal treatment, acid treatment, metal doping, heteroatom doping, etc.

Heteroatom doping is a technique that introduces atoms of different elements, such as nitrogen (N), boron (B), phosphorus (P) and sulfur (S) into the lattice of carbon materials as heteroatom dopants [12,13]. This technique can effectively tune the intrinsic properties of carbon materials, and it has been widely used in many energy storage systems [14-16]. In VRFBs, the first attempt to utilize an N-doped carbon electrode may be attributed to Shao et al. [17]. They prepared mesoporous carbon electrode via a softtemplate method and the nitrogen was doped by heat treating the electrode in NH<sub>3</sub>. The electrocatalytic kinetics and reversibility of  $VO_2^{+}/VO_2^{+}$  was found to be enhanced. They explained that Ndoping facilitates the electron transfer on electrode/electrolyte interface for both oxidation and reduction process. Later, Wu et al. [18] developed N-doped graphite felt as the electrode material via hydrothermal ammoniated treatment. In addition to doping N into mesoporous carbon and graphite felt electrodes, Wang et al. [19] developed N-doped carbon nanotubes with graphite felt substrates as electrodes for VRFBs using chemical vapor deposition method.





They explained that the improved cell performance originated from the modified electronic properties and increased surface oxygen species of the carbon nanotubes as the result of N-doping. To identify the role of nitrogen species for the  $VO_2^{+}/VO_2^{+}$  couple reaction, Jin et al. [20] synthesized N-doped graphene sheets by annealing graphite oxide with urea. They proposed that the enhanced catalytic activity for  $VO_2^{+}/VO_2^{+}$  reaction resulted from the change of electron density and newly created localized states, which facilitated the adsorption of  $VO_2^{+}/VO_2^{+}$  ions on nitrogen dopant and conjugation of electron of reaction into these localized states. They further confirmed that not the nitrogen doping level but the nitrogen type in the graphene sheets determined the catalytic activity, and the quaternary-N species provide more active sites and a catalyst for the  $VO_2^+/VO_2^+$  redox reaction. Shi et al. [21] further proved that the quaternary-N plays the main role in accelerating the  $VO_2^+/VO_2^+$  redox reactions. Their graphene nanosheets electrodes were prepared through hydrothermal reaction with urea as the nitrogen source, and the nitrogen species could be turned by controlling the hydrothermal reaction time.

The above studies focused on utilizing N-doped carbon

Table 1	
Structure parameters of pristine graphene and N-, B-, P-doped graphene.	

	a (Å)	b (Å)
pristine graphene	9.8564	12.8236
graphitic N-doped graphene	9.8526	12.8130
hydrogenated pyridinic N-doped graphene	9.8654	12.8353
hydrogenated pyrrolic N-doped graphene	9.8254	12.9431
graphitic B-doped graphene	9.8999	12.8747
graphitic P-doped graphene	9.8942	12.8672

electrodes in VRFBs, while efforts on adopting B- and P-doped carbon electrodes in VRFBs have also been made. For example, Shi et al. [22] prepared B- or N- mono-doped carbon nanofiber electrodes by electrospinning method. Improved electrochemical performance for the  $VO^{2+}/VO_2^+$  redox reaction was observed. In addition, they investigated B and N co-doped carbon nanofiber electrodes with separated case and bonded case. They concluded that not the total amount of incorporated B and N but how the B and N are incorporated into carbon nanostructures determines the catalytic activity toward  $VO^{2+}/VO_2^+$  redox reaction. He et al. [23] prepared N-, P-, co-doped carbon microsphere electrodes by hydrothermal treatment followed by calcination with  $(NH_4)_2HPO_4$  as N and P sources. The superior electrochemical performance was ascribed to the increased total number of heteroatoms as active sites and synergistic effect of N- and P- co-doping.

Despite numerous experimental investigations on the heteroatom doping in VRFBs, there lacks comprehensive comparison of heteroatom-doped carbon electrodes with different elements. In this work, we present first-principle investigations on the adsorption-desorption behavior of aqueous  $V^{2+}/V^{3+}$  redox species on the basal plane of nitrogen, boron and phosphorus doped graphite electrode surface. Because graphite consists of single graphene layers connected via van der Waals force, graphene layer is chosen to represent the basal plane of graphite electrode for simplicity [24–26]. Our computational results promote the understanding of  $V^{2+}/V^{3+}$  redox reaction and provide in-depth insight into the heteroatom doping of carbon electrodes in VRFBs.

#### 2. Computational details

DFT computations were performed based on plane-wave



**Fig. 1.** Top and side view of the atomic structure of (a) pristine graphene, (b) graphitic N-doped graphene, (c) hydrogenated pyridinic N-doped graphene, (d) hydrogenated pyrrolic N-doped graphene, (e) graphitic B-doped graphene, and (f) graphitic P-doped graphene.

technique implemented in the ABINIT software package (version 8.6.3) [27–31]. Projector-augmented plane wave (PAW) pseudopotentials were used to describe the ion-electron interactions [32]. A generalized gradient approximation (GGA) expressed by the Perdew-Burke-Ernzerhof (PBE) functional was adopted to treat the exchange-correlation functional [33]. To describe the van der Waals interaction, Grimme's D2 correction was adopted [34]. The cutoff energy for the plane-wave basis was set to be 20 Ha. For geometrical optimization, the force tolerance was set to be 0.02 eV/Å. A uniform compensating background was added to restore the charge neutrality.

The graphene substrate expands along the *a* and *b* directions  $(a \approx 9.9 \text{ Å}, b \approx 12.8 \text{ Å}, \text{ detailed values of } a \text{ and } b \text{ for each graphene}$ substrate is given in Table 1); the vacuum space in the *c* direction was set to be 20 Å to avoid any interlayer interactions. Integrations over the Brillouin zones were sampled with a  $3 \times 2 \times 1$  mesh of uniformly spaced k points such that the k-point mesh is less than 0.05 Å<sup>-1</sup>. For density of states (DOS) calculation, a denser k-point mesh less than 0.02 Å<sup>-1</sup> was used. To calculate the water adsorption energy, a cubic supercell of length 10 Å containing a single H<sub>2</sub>O molecule was constructed and only the Gamma point was sampled in the Brillouin zone. The adsorption energy is then calculated as  $E_{ads} = E_{total} - E_{substrate} - E_{H_2O}$ , where  $E_{total}$ ,  $E_{substrate}$  and  $E_{H_2O}$  represent the energy of the total system, the graphene substrate and the water adsorbate, respectively. To prepare the hydration shell geometry of aqueous  $V(H_2O)_6^{2+}$  and  $V(H_2O)_6^{3+},$  a cubic supercell of length 20 Å containing one V atom and six H<sub>2</sub>O molecules was constructed, and only the Gamma point was sampled in the Brillouin zone.

# 3. Results and discussion

According to previous investigations of N-doped, B-doped and P-doped graphene, there are three kinds of in-plane N configurations (i.e., graphitic N-dope, pyridinic N-dope, and pyrrolic Ndope), one kind of in-plane B configuration (i.e., graphitic B-dope) and one kind of in-plane P configuration (i.e., graphitic P-dope) in the lattice of graphene [13,35]. The atomic structures in this study are shown in Fig. 1. The graphitic N-, B-, and P- doped graphene is built by replacing one C atom with a N. B. and P atom, respectively. In the graphitic N- and B-doped graphene, all atoms are in one plane; while in the graphitic P-doped graphene, the P atom protrudes out of the graphene plane. For pyridinic N-doped and pyrrolic N-doped graphene, we found that for the cases without hydrogenation or with only one hydrogen atom included, the interaction between graphene substrate and water molecules is so strong that the O-H bond in water molecules will be tear apart and new N-H bond will be formed. This phenomenon indicates that bare pyridinic N-doped or pyrrolic N-doped graphene is highly unstable in aqueous environment and will be transferred into hydrogenated configurations quickly. Thus, we adopted hydrogenated configurations with two hydrogen atoms in our computations. For the hydrogenated pyridinic N-doped graphene, the H atoms protrudes out of the graphene plane, as shown in Fig. S1. This configuration is more stable compare to the configuration where all atoms sits in one plane, since its total energy difference is 0.158 eV



**Fig. 2.** Water adsorption configurations on (a) pristine graphene, (b) graphitic N-doped graphene, (c) hydrogenated pyridinic N-doped graphene, (d) hydrogenated pyrrolic N-doped graphene, (e) graphitic B-doped graphene, and (f) graphitic P-doped graphene.



Fig. 3. (a) Water adsorption energies and (b) the distances between water and graphene surfaces.

lower. The electron distribution map for graphene doped with different elements are provided in Fig. S2.

We first calculate the water adsorption energies and the distances between  $H_2O$  and different graphene surfaces to evaluate the wettability of carbon electrode surface. The detailed adsorption configurations are given in Fig. 2. Three adsorption modes were considered in our computations [36–38]. From Fig. 3, we can see that the adsorption energy for isolated  $H_2O$  molecule on monolayer pristine graphene is around 0.13 eV, which is consistent with previous works [38–40]. The absolute values of all the adsorption energies are smaller than 0.3 eV; the optimized distances between the oxygen atom of  $H_2O$  molecule and graphene surfaces are all larger than 2.5 Å (for the case of graphitic P-doped graphene, we calculate the distance between oxygen atom and phosphorus atom since the basal graphene plane is distorted). In addition, for the hydrogenated pyridinic N-doped and pyrrolic N-doped graphene,



**Fig. 4.** Density of states of (a) pristine graphene, (b) graphitic N-doped graphene, (c) hydrogenated pyridinic N-doped graphene, (d) hydrogenated pyrrolic N-doped graphene, (e) graphitic B-doped graphene, and (f) graphitic P-doped graphene.

the water adsorption energies are larger, and the distances between water and graphene surfaces are shorter. On the other hand, the water adsorption mode is still physisorption rather than chemisorption as indicated in Fig. 3. Overall, these results indicate the interactions between H<sub>2</sub>O and graphene surfaces are mainly weak van der Waals forces. We then calculate the density of states (DOS) for different graphene surfaces. As shown in Fig. 4, all the heteroatom doped surfaces under consideration can preserve their metallic features well, which ensures the high electronic conductivity of the carbon electrode in VRFBs.

The optimized first coordination sphere of aqueous  $V(H_2O)_6^{2+}$ and  $V(H_2O)_6^{3+}$  and their corresponding structure parameters are given in Fig. 5 and Table 2, respectively. Fig. 6 illustrates the adsorption modes of  $V^{2+}$  and  $V^{3+}$  ions on pristine graphene. Here, we consider one inner-sphere adsorption mode and three outersphere adsorption modes. The inner-sphere adsorption mode is built by placing one water molecule into the second coordination



Fig. 5. First coordination sphere of aqueous vanadium ions: (a)  $V(H_2O)_6^{2+};$  (b)  $V(H_2O)_6^{3+}.$ 

Table 2
Structural parameters of $V(H_2O)_6^{2+}$ and $V(H_2O)_6^{3+}$ .

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Method	$V^{2+}$ (R <sub>V-0</sub> , Å)	$V^{3+}$ ( $R_{V-0}$ , Å)
Present	2.124	2.039
CPMD [44]	2.23	2.10
B3LYP [42]	2.21	2.09
HF [45]	2.20	2.06
XRD [46,47]	2.13	2.00



Fig. 6. Adsorption modes of  $V(H_2O)_6^{2+}$  and  $V(H_2O)_6^{3+}$  on pristine graphene surfaces.

sphere; the three outer-sphere adsorption modes are built based on the T<sub>h</sub> symmetry of the V(H<sub>2</sub>O)<sub>6</sub><sup>2+</sup> and V(H<sub>2</sub>O)<sub>6</sub><sup>3+</sup>. Hirshfeld charge analysis [41] and V–O bond lengths for isolated and adsorbed V(H<sub>2</sub>O)<sub>6</sub><sup>2+</sup>/V(H<sub>2</sub>O)<sub>6</sub><sup>3+</sup> on pristine graphene surface are provided in Figs. S3–S12. Similar adsorption modes of V(H<sub>2</sub>O)<sub>6</sub><sup>2+</sup> and V(H<sub>2</sub>O)<sub>6</sub><sup>3+</sup> adsorbed on N-, B-, and P-doped graphene surfaces are considered in the following discussion.

The charge transfer for  $V^{2+}$  ions and  $V^{3+}$  ions adsorbed on pristine graphene surfaces are shown in Figs. 7 and 8, respectively. From the charge transfer map, we can clearly observe that the charge transfer between vanadium ions and graphene surfaces are mainly conducted via inner-sphere adsorption mode. Since outsphere modes mainly exist in bulk electrolyte solution and the redox reaction of  $V^{2+}/V^{3+}$  is a simple one-electron transfer process,



Fig. 8. Charge transfer of V<sup>3+</sup> ions adsorbed on the pristine graphene surfaces.

the stabilization of the inner-sphere adsorption mode will directly contribute to the reaction kinetics and enhance the catalytic activity [9,42,43]. Thus, in the following, we will adopt the metrics of  $\Delta E = E_{\text{inner}} - E_{\text{outer}}$  to quantify the ability of the graphene surfaces to facilitate the transformation of V<sup>2+</sup>/V<sup>3+</sup> adsorption modes from the outer-sphere mode to the inner-sphere mode.

The energy difference between the inner-sphere adsorption and outer-sphere adsorption modes for  $V^{2+}/V^{3+}$  ions on different kinds of surfaces are shown in Fig. 9. From the results, we can see that on pristine graphene surface, the formation of inner-sphere adsorption mode for  $V^{3+}$  ions are harder than that for  $V^{2+}$  ions, which is consistent with the experimental observation that  $V^{3+}$  ions show sluggish reaction kinetics. It is also found that graphitic N-doped graphene will slightly facilitate the formation of inner-sphere mode for  $V^{2+}$ , while pyridinic N-doped graphene surface will enhance its activity towards  $V^{3+}$ . This indicates that different kinds of N atom doping may play different roles in the redox reaction of  $V^{2+}/V^{3+}$ . For B-doped graphene surface, its catalytic activity towards  $V^{3+}$  ions is more prominent. An interesting finding is that for P-doped



Fig. 7. Charge transfer of  $V^{2+}$  ions adsorbed on the pristine graphene surfaces.



Fig. 9. The energy difference between the inner-sphere and outer-sphere adsorption modes for  $V^{2+}$  and  $V^{3+}$  ions on different graphene surfaces.

graphene surface, the catalytic activity towards both  $V^{2+}$  and  $V^{3+}$ ions can be significantly improved. Although limited experimental efforts have been focused on the P-doped graphite as the electrodes for VRFBs, here our theoretical work suggests a promising method for developing graphite electrodes for VRFBs.

#### 4 Conclusions

In this work, we provide a comprehensive exploration on the feasibility of N-, B-, and P-doped graphite as electrodes for VRFBs via density functional theory calculations. The main findings are summarized as follows:

- 1. The water interaction is stronger with hydrogenated pyridinic N-doped and pyrrolic N-doped graphene than that of graphitic N-, B- and P-doped graphene, while the density of state of all the modified graphene remains metallic features. These indicate the good wettability and electronic conductivity of heteroatom doped graphite electrodes for VRFBs.
- 2. Graphitic N-doped graphene will slightly facilitate the formation of inner-sphere mode for  $V^{2+}$ , while pyridinic N-doped graphene surface will enhance its activity towards V<sup>3+</sup>. For Bdoped graphene surface, its catalytic activity towards V<sup>3+</sup> ions is more prominent. For P-doped graphene surface, its catalytic activity towards both  $V^{2+}$  and  $V^{3+}$  ions can be significantly improved. Future research efforts may be focused on utilizing Pdoped graphite as electrodes for VRFBs.

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# Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.electacta.2019.01.109.

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